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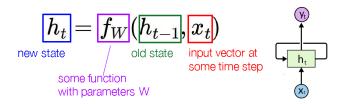
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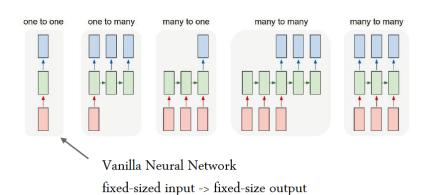
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 - Text generation
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- The clouds are in the ?
 - sky
- Simple solution: N-grams?
 - Hard to represent patterns with more than a few words (possible patterns increases exponentially)
- Simple solution: Neural networks?
 - Fixed input/output size
 - Fixed number of steps

Recurrent Neural Networks

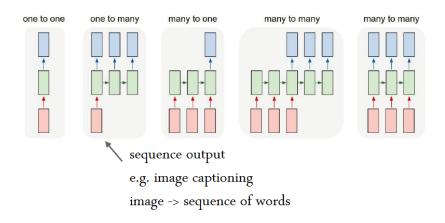
 Recurrent neural networks (RNNs) are networks with loops, allowing information to persist [Rumelhart et al., 1986].

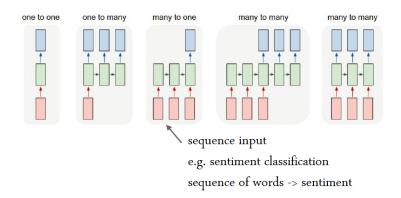


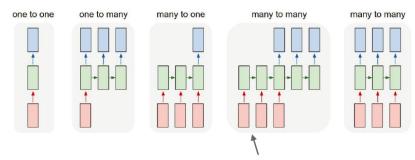
- Have memory that keeps track of information observed so far
- Maps from the entire history of previous inputs to each output
- Handle sequential data



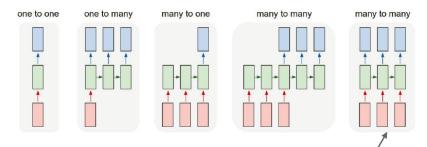
e.g. image classification







sequence input and sequence output e.g. machine translation seq of words -> seq of words



synced sequence input and output e.g. video classification on frame level

Sequential Processing in Absence of Sequences

 Even if inputs/outputs are fixed vectors, it is still possible to use RNNs to process them in a sequential manner.

Sequential Processing of fixed inputs





Multiple Object Recognition with Visual Attention, Ba et al.

Recurrent Neural Networks

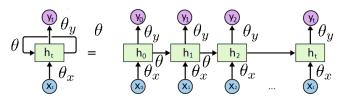
$$\mathbf{h}_{t} = \theta \phi(\mathbf{h}_{t-1}) + \theta_{x} \mathbf{x}_{t}$$

$$\mathbf{y}_{t} = \theta_{y} \phi(\mathbf{h}_{t})$$

- \mathbf{x}_t is the **input** at time t.
- \mathbf{h}_t is the **hidden state** (memory) at time t.
- y_t is the **output** at time t.
- θ , θ_x , θ_y are distinct **weights**.
 - weights are the same at all time steps.

Recurrent Neural Networks

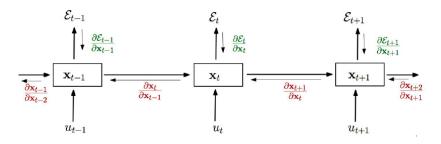
 RNNs can be thought of as multiple copies of the same network, each passing a message to a successor.



- The same function and the same set of parameters are used at every time step.
 - Are called recurrent because they perform the same task for each input.

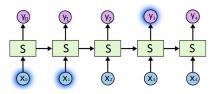
Back-Propagation Through Time (BPTT)

- Using the generalized back-propagation algorithm one can obtain the so-called Back-Propagation Through Time algorithm.
- The recurrent model is represented as a multi-layer one (with an unbounded number of layers) and backpropagation is applied on the unrolled model.

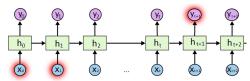


The Problem of Long-term Dependencies

- RNNs connect previous information to present task:
 - may be enough for predicting the next word for "the clouds are in the sky"



 may not be enough when more context is needed: "I grew up in France ... I speak fluent French"

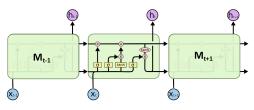


Vanishing/Exploding Gradients

- In RNNs, during the gradient back propagation phase, the gradient signal can end up being multiplied many times.
- If the gradients are large
 - Exploding gradients, learning diverges
 - Solution: clip the gradients to a certain max value.
- If the gradients are small
 - Vanishing gradients, learning very slow or stops
 - Solution: introducing memory via LSTM, GRU, etc.

Long Short-Term Memory Networks

 Long Short-Term Memory (LSTM) networks are RNNs capable of learning long-term dependencies [Hochreiter and Schmidhuber, 1997].



- A memory cell using logistic and linear units with multiplicative interactions:
 - Information gets into the cell whenever its input gate is on.
 - Information is thrown away from the cell whenever its forget gate is off.
 - Information can be read from the cell by turning on its output gate.

LSTM Overview

- We define the LSTM unit at each time step t to be a collection of vectors in \mathbb{R}^d :
 - Memory cell c_t

$$\widetilde{\mathbf{c}_t} = \mathsf{Tanh}(W_c.[\mathbf{h}_{t-1},\mathbf{x}_t] + \mathbf{b}_c)$$
 vector of new candidate values $\mathbf{c}_t = \mathbf{f}_t * \mathbf{c}_{t-1} + \mathbf{i}_t * \widetilde{\mathbf{c}}_t$

• Forget gate f_t in [0, 1]: scales old memory cell value (reset)

$$\mathbf{f}_t = \sigma(W_f.[\mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_f)$$

Input gate i_t in [0, 1]: scales input to memory cell (write)

$$\mathbf{i}_t = \sigma(W_i.[\mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_i)$$

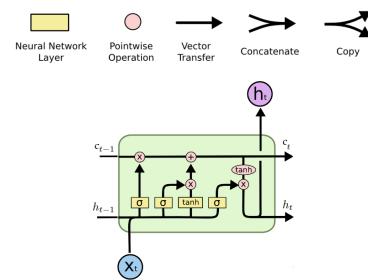
• Output gate o_t in [0, 1]: scales output from memory cell (read)

$$\mathbf{o}_t = \sigma(W_o.[\mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_o)$$

Output h_t

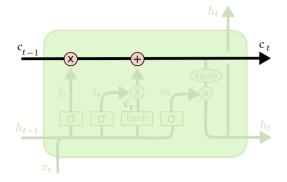
$$\mathbf{h}_t = \mathbf{o}_t * \mathsf{Tanh}(\mathbf{c}_t)$$

Notation



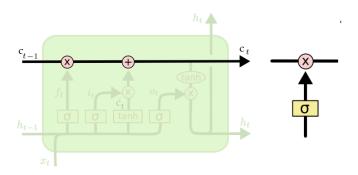
The Core Idea Behind LSTMs: Cell State (Memory Cell)

- Information can flow along the memory cell unchanged.
- Information can be removed or written to the memory cell, regulated by gates.



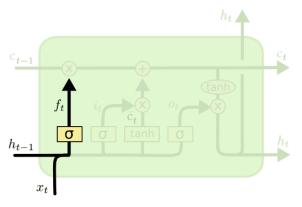
Gates

- Gates are a way to optionally let information through.
 - A sigmoid layer outputs number between 0 and 1, deciding how much of each component should be let through.
 - A pointwise multiplication operation applies the decision.



Forget Gate

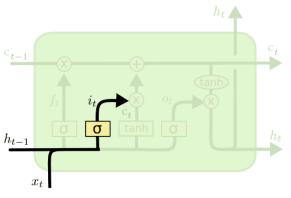
 A sigmoid layer, forget gate, decides which values of the memory cell to reset.



$$\mathbf{f}_t = \sigma(W_f.[\mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_f)$$

Input Gate

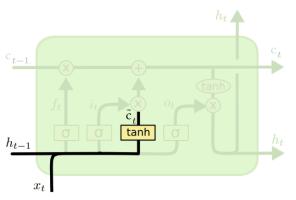
 A sigmoid layer, input gate, decides which values of the memory cell to write to.



$$\mathbf{i}_t = \sigma(W_i.[\mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_i)$$

Vector of New Candidate Values

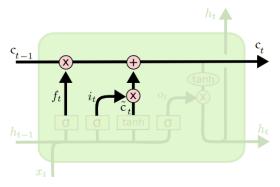
• A Tanh layer creates a vector of new candidate values $\widetilde{\mathbf{c}}_t$ to write to the memory cell.



$$\widetilde{\mathbf{c}}_t = \mathsf{Tanh}(W_c.[\mathbf{h}_{t-1},\mathbf{x}_t] + \mathbf{b}_c)$$

Memory Cell Update

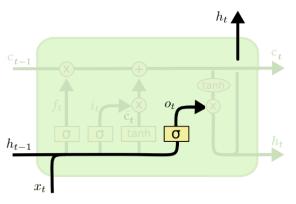
- The previous steps decided which values of the memory cell to reset and overwrite.
- Now the LSTM applies the decisions to the memory cell.



$$\mathbf{c}_t = \mathbf{f}_t * \mathbf{c}_{t-1} + \mathbf{i}_t * \widetilde{\mathbf{c}}_t$$

Output Gate

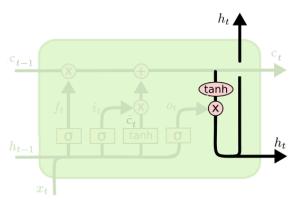
 A sigmoid layer, output gate, decides which values of the memory cell to output.



$$\mathbf{o}_t = \sigma(W_o.[\mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_o)$$

Output Update

 The memory cell goes through Tanh and is multiplied by the output gate.



$$\mathbf{h}_t = \mathbf{o}_t * \mathsf{Tanh}(\mathbf{c}_t)$$

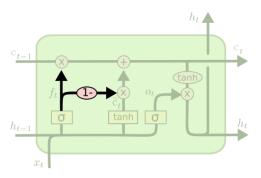
Variants on LSTM

 Gate layers look at the memory cell [Gers and Schmidhuber, 2000].

$$\mathbf{f}_t = \sigma(W_f.[\mathbf{c}_{t-1}, \mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_f)$$
 $\mathbf{i}_t = \sigma(W_i.[\mathbf{c}_{t-1}, \mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_i)$
 $\mathbf{o}_t = \sigma(W_o.[\mathbf{c}_{t-1}, \mathbf{h}_{t-1}, \mathbf{x}_t] + \mathbf{b}_o)$
 \mathbf{h}_{t-1}

Variants on LSTM

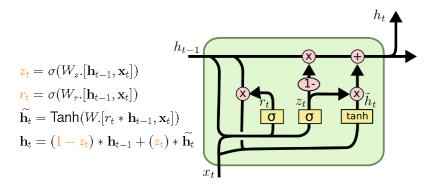
 Use coupled forget and input gates. Instead of separately deciding what to forget and what to add, make those decisions together.



$$\mathbf{c}_t = \mathbf{f}_t * \mathbf{c}_{t-1} + (1 - \mathbf{f}_t) * \widetilde{\mathbf{c}}_t$$

Variants on LSTM

- Gated Recurrent Unit (GRU) [Cho et al., 2014]:
 - Combine the forget and input gates into a single update gate.
 - Merge the memory cell and the hidden state.
 - ...



Applications

- Cursive handwriting recognition
 - https://www.youtube.com/watch?v=mLxsbWAYIpw
- Translation
 - Translate any signal to another signal, e.g., translate English to French, translate image to image caption, and songs to lyrics.
- Visual sequence tasks

