

# CYK parsing

# The task

*Constituency (or constituent) parsing* refers to recovering the derivational structure of a sentence, usually assuming it was generated by a context-free grammar.

Shieber (1986) shows, conclusively, that human language is not even weakly context-free; and one can parse using *mildly context-sensitive grammars* (MCSGs), such as

- lexicalized tree-adjoining grammars (LTAGs) or
- combinatory categorial grammar (CCGs).

CFGs can be parsed in  $O(n^3)$  or better; MCSGs can be parsed in  $O(n^6)$ .

# Ambiguity

Non-trivial CFGs tend to have substantial ambiguities, so we use:

- *Probabilistic* productions, making the grammar a PCFG and parsing a special case of the Viterbi algorithm
- Learned (e.g., Klein & Manning 2003) or induced (e.g., Petrov et al. 2006) enrichments to the productions to encode argument structure of verbs, etc.
- Optionally, discriminative reranking (e.g., Collins 1999, Bikel 2004)

None of these has a major impact on the actual parsing algorithm, however.

# Structural ambiguity: prepositional phrase attachment

*Pope Francis **on** Saturday appointed a victim **of** sexual abuse and a senior cardinal known **for** his zero-tolerance approach **to** a new group charged **with** advising the Catholic Church **on** how to respond **to** the problem **of** sexual abuse **of** children. (Wall St. Journal, 2014-03-22)*

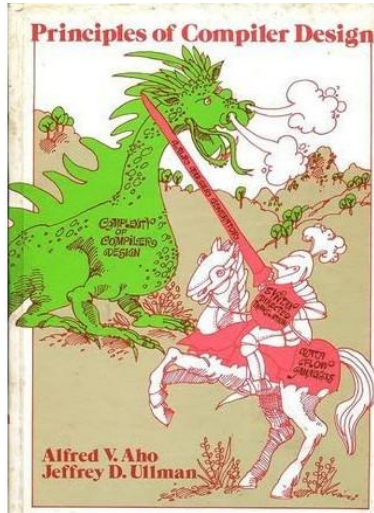
- The prepositional phrase *on Saturday* is construed as a modifier of *Pope Francis* rather than of *appointed*.
- The phrase *to a new group charged with advising the Catholic Church on how to respond to the problem of sexual abuse of children* is construed as a modifier of *zero tolerance approach* rather than of *appointed*.

# CFGs and compilers

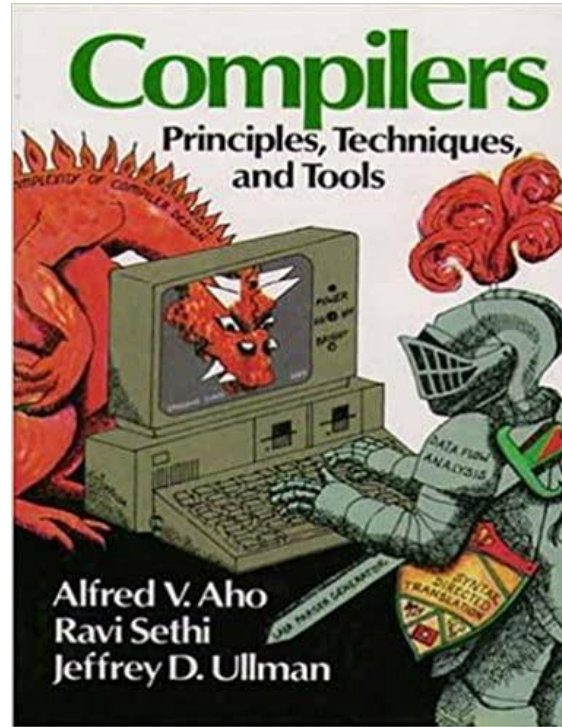
CFG parsing has been studied *extensively* for compiler design long before it was used to parse natural language.

Computer languages are designed to be unambiguous or even deterministic, and compiler designers can take advantages of more-efficient algorithms for these special cases (e.g., the Earley algorithm, the LL and LALR parsers, etc.).

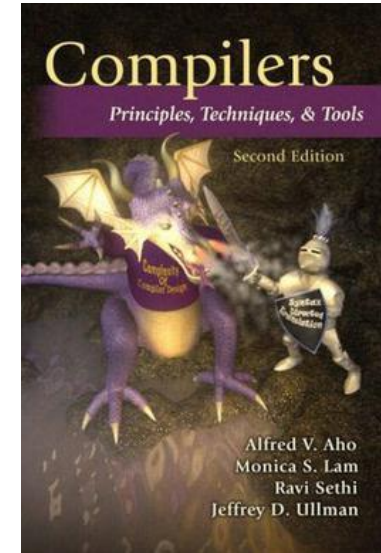
Probably the best known parsing algorithm for natural language is the [simultaneously-invented](#) Cocke-Younger-Kasami (CYK or CKY) algorithm, a simple bottom-up parsing algorithm.



Aho & Ullman 1977



Aho, Sethi & Ullman 1986



Aho, Lam, Sethi & Ullman 2006

# Example grammar

```
S → NP VP
VP → VP PP      # Permits PPs to adjoin to VP.
VP → V NP       # Permits transitive VPs.
VP → V          # Permits intransitive VPs.
PP → P NP
NP → D N        # Permits article-noun NPs.
NP → NP PP      # Permits PPs to adjoin to NP.
NP → N          # Permits bare NPs.
NP → Pagliaccio
V → eats
N → spaghetti | fork
P → with
D → a
```

# Eliminate unary productions

Before:

VP → V  
NP → N

After:

VP → eats  
NP → spaghetti, fork



# Grammar representation structure

The preterminal rules are simple mappings, and only used once.

```
preterminals: Dict[str, List[str]]
```

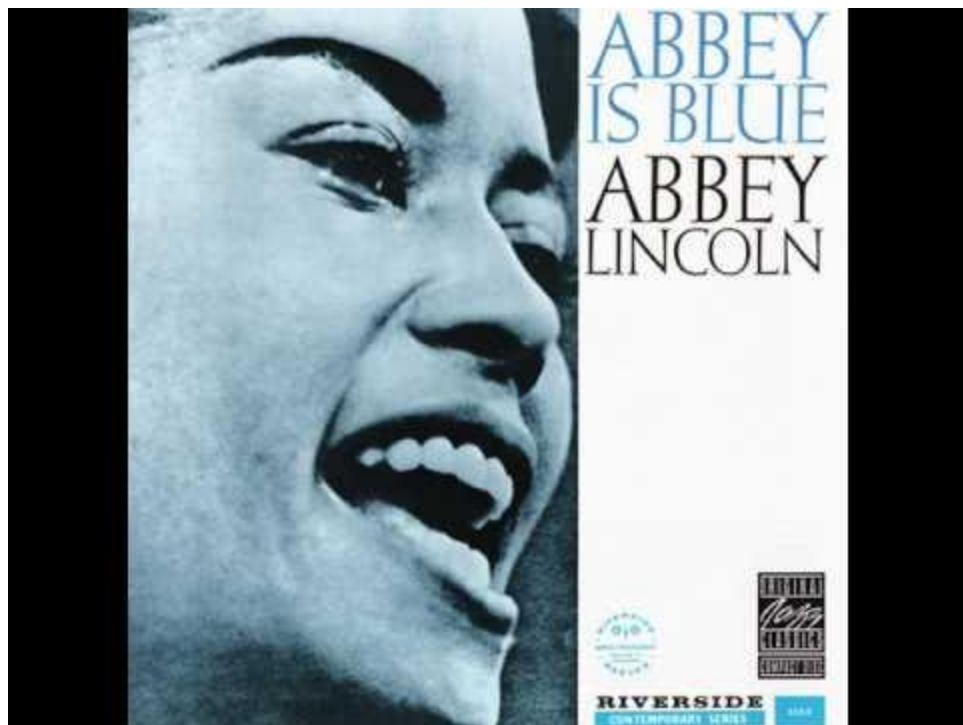
The non-terminal rules map from pairs of strings (the children/daughters/productions) to non-terminals.

```
nonterminals: Dict[Tuple[str, str], List[str]]
```

Looking up productions to find candidate non-terminals is known as *grammar intersection*. Intersection is performed  $O(n^3)$  times, so it *has* to be constant-time.

*Pagliaccio eats spaghetti  
with a fork*

(Do you see the ambiguity?)



# The ambiguity

1. Pagliaccio [<sub>VP</sub> [<sub>VP</sub> eats spaghetti] [with a fork] ]

(The fork is an instrument for eating.)

2. Pagliaccio eats [<sub>NP</sub> [<sub>NP</sub> spaghetti] [with a fork] ]

(The fork is a tasty topping for the spaghetti.)

# The CYK chart

Given a sentence of length  $n$ , construct an  $n \times n$  table, empty above the diagonal, in which each cell is a container of non-terminal labels.

For efficient memory use you **might** want to construct a `Chart` class that has-a  $n \times n / 2 + 1$  array and overloads `__getitem__` and `__setitem__` so you can **pretend** you really do have a  $n \times n$  table without wasting the extra space.

(If you find an error in the  
demo, let me know.)

Initial chart (plus an extra row at the bottom, for display)

|            |      |           |      |   |      |
|------------|------|-----------|------|---|------|
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
| Pagliaccio | eats | spaghetti | with | a | fork |

# Insert preterminals

|            |      |           |      |   |      |
|------------|------|-----------|------|---|------|
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
| NP         | VP   | NP        | P    | D | NP   |
| Pagliaccio | eats | spaghetti | with | a | fork |



# Size 2 spans

|            |           |           |      |   |      |
|------------|-----------|-----------|------|---|------|
|            |           |           |      |   |      |
|            |           |           |      |   |      |
|            |           |           |      |   |      |
|            |           |           |      |   |      |
| <b>S</b>   |           |           |      |   |      |
| <b>NP</b>  | <b>VP</b> | NP        | P    | D | NP   |
| Pagliaccio | eats      | spaghetti | with | a | fork |

# Size 2 spans

|            |      |           |      |   |      |
|------------|------|-----------|------|---|------|
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
| S          | VP   |           |      |   |      |
| NP         | VP   | NP        | P    | D | NP   |
| Pagliaccio | eats | spaghetti | with | a | fork |

# Size 2 spans

|            |      |           |      |   |      |
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|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
| S          | VP   |           |      |   |      |
| NP         | VP   | NP        | P    | D | NP   |
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|            |      |           |      |   |      |
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|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
| S          | VP   |           |      |   |      |
| NP         | VP   | NP        | P    | D | NP   |
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|            |      |           |      |           |           |
|------------|------|-----------|------|-----------|-----------|
|            |      |           |      |           |           |
|            |      |           |      |           |           |
|            |      |           |      |           |           |
|            |      |           |      |           |           |
| S          | VP   |           |      | <b>NP</b> |           |
| NP         | VP   | NP        | P    | <b>D</b>  | <b>NP</b> |
| Pagliaccio | eats | spaghetti | with | a         | fork      |

# Size 3 spans

|            |           |           |      |    |      |
|------------|-----------|-----------|------|----|------|
|            |           |           |      |    |      |
|            |           |           |      |    |      |
|            |           |           |      |    |      |
| <b>S</b>   |           |           |      |    |      |
| S          | <b>VP</b> |           |      | NP |      |
| <b>NP</b>  | VP        | NP        | P    | D  | NP   |
| Pagliaccio | eats      | spaghetti | with | a  | fork |

# Size 3 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           |      |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 3 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           |      |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |



# Size 3 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           |      |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

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|            |      |           |      |   |      |
|------------|------|-----------|------|---|------|
|            |      |           |      |   |      |
|            |      |           |      |   |      |
|            |      |           |      |   |      |
| S          |      |           |      |   |      |
| S          | VP   |           |      |   | NP   |
| NP         | VP   | NP        | P    | D | NP   |
| Pagliaccio | eats | spaghetti | with | a | fork |

# Size 3 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           |      |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 3 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 3 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 4 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 4 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 4 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |



# Size 4 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

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|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 4 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 4 spans

|            |      |           |      |    |      |    |
|------------|------|-----------|------|----|------|----|
|            |      |           |      |    |      |    |
|            |      |           |      |    |      |    |
|            |      | NP        |      |    |      |    |
| S          |      |           | PP   |    |      |    |
| S          | VP   |           |      | NP |      |    |
| NP         | VP   | NP        |      | P  | D    | NP |
| Pagliaccio | eats | spaghetti | with | a  | fork |    |

(This is the NP-adjunction analysis.)

# Size 4 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      | NP        |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 4 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      | NP        |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 5 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      | NP        |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 5 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      | NP        |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |



# Size 5 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      | NP        |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 5 spans

|            |      |           |      |    |      |
|------------|------|-----------|------|----|------|
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      |           |      |    |      |
|            |      | NP        |      |    |      |
| S          |      |           | PP   |    |      |
| S          | VP   |           |      | NP |      |
| NP         | VP   | NP        | P    | D  | NP   |
| Pagliaccio | eats | spaghetti | with | a  | fork |

# Size 5 spans

|            |           |           |      |    |      |
|------------|-----------|-----------|------|----|------|
|            |           |           |      |    |      |
|            | <b>VP</b> |           |      |    |      |
|            |           | <b>NP</b> |      |    |      |
| S          |           |           | PP   |    |      |
| S          | VP        |           |      | NP |      |
| NP         | <b>VP</b> | NP        | P    | D  | NP   |
| Pagliaccio | eats      | spaghetti | with | a  | fork |

(This is the NP-adjunction analysis.)

# Size 5 spans

|            |        |           |      |    |      |
|------------|--------|-----------|------|----|------|
|            |        |           |      |    |      |
|            | VP, VP |           |      |    |      |
|            |        | NP        |      |    |      |
| S          |        |           | PP   |    |      |
| S          | VP     |           |      | NP |      |
| NP         | VP     | NP        | P    | D  | NP   |
| Pagliaccio | eats   | spaghetti | with | a  | fork |

(This is the VP-adjunction analysis.)

# Size 5 spans

|            |        |           |      |    |      |
|------------|--------|-----------|------|----|------|
|            |        |           |      |    |      |
|            | VP, VP |           |      |    |      |
|            |        | NP        |      |    |      |
| S          |        |           | PP   |    |      |
| S          | VP     |           |      | NP |      |
| NP         | VP     | NP        | P    | D  | NP   |
| Pagliaccio | eats   | spaghetti | with | a  | fork |

# Size 5 spans

|            |        |           |      |    |      |
|------------|--------|-----------|------|----|------|
|            |        |           |      |    |      |
|            | VP, VP |           |      |    |      |
|            |        | NP        |      |    |      |
| S          |        |           | PP   |    |      |
| S          | VP     |           |      | NP |      |
| NP         | VP     | NP        | P    | D  | NP   |
| Pagliaccio | eats   | spaghetti | with | a  | fork |

# Size 6 spans

|             |               |           |      |    |      |
|-------------|---------------|-----------|------|----|------|
| <b>S, S</b> |               |           |      |    |      |
|             | <b>VP, VP</b> |           |      |    |      |
|             |               | NP        |      |    |      |
| S           |               |           | PP   |    |      |
| S           | VP            |           |      | NP |      |
| <b>NP</b>   | VP            | NP        | P    | D  | NP   |
| Pagliaccio  | eats          | spaghetti | with | a  | fork |

# Size 6 spans

|            |        |           |      |    |      |
|------------|--------|-----------|------|----|------|
| S, S       |        |           |      |    |      |
|            | VP, VP |           |      |    |      |
|            |        | NP        |      |    |      |
| S          |        |           | PP   |    |      |
| S          | VP     |           |      | NP |      |
| NP         | VP     | NP        | P    | D  | NP   |
| Pagliaccio | eats   | spaghetti | with | a  | fork |



# Size 6 spans

|            |        |           |      |    |      |
|------------|--------|-----------|------|----|------|
| S, S       |        |           |      |    |      |
|            | VP, VP |           |      |    |      |
|            |        | NP        |      |    |      |
| S          |        |           | PP   |    |      |
| S          | VP     |           |      | NP |      |
| NP         | VP     | NP        | P    | D  | NP   |
| Pagliaccio | eats   | spaghetti | with | a  | fork |

# Size 6 spans

|            |        |           |      |    |      |
|------------|--------|-----------|------|----|------|
| S, S       |        |           |      |    |      |
|            | VP, VP |           |      |    |      |
|            |        | NP        |      |    |      |
| S          |        |           | PP   |    |      |
| S          | VP     |           |      | NP |      |
| NP         | VP     | NP        | P    | D  | NP   |
| Pagliaccio | eats   | spaghetti | with | a  | fork |

# Size 6 spans

|            |        |           |      |    |      |
|------------|--------|-----------|------|----|------|
| S, S       |        |           |      |    |      |
|            | VP, VP |           |      |    |      |
|            |        | NP        |      |    |      |
| S          |        |           | PP   |    |      |
| S          | VP     |           |      | NP |      |
| NP         | VP     | NP        | P    | D  | NP   |
| Pagliaccio | eats   | spaghetti | with | a  | fork |

## Recognition vs. parsing

When there an S in the top-left cell of the chart, the sentence is *recognized* by the grammar; i.e., there is at least one complete parse of the sentence.

To actually *parse* (and to extract the parses), we have to keep backtraces similar to Viterbi decoding.

# Generalizing to PCFGs

Whereas above each cell was a container of non-terminals, in PCFG parsing each cell is a container of triples of;

1. non-terminal
2. log-probability
3. backtraces

Much like with the Viterbi algorithm, we obtain the **highest-probability parse** by tracing back from the **highest-probability S-triple in the top-left cell**.

# Data

Unlike dependency parsing (the subject of next week's lecture), constituency parsing treebanks are available for maybe a dozen languages, and many are proprietary. Two widely studied ones are:

- English: The Wall St. Journal portion of the Penn Treebank, 3rd edition (Marcus et al. 1999; first release was 1993, I think)
- German: The Tiger2 corpus (Brants et al. 2002)

For German, which is "morphologically rich and less-configurational", it is generally agreed that parsing is poor without the assistance of a high-quality morphological analyzer (e.g., Dubey 2005, Fraser et al. 2013, Dehouck and Denis 2018).

# Evaluation

Parsing performance is usually evaluated using the  $F$ -score of the constituents:

- Precision: the number of the constituents in the candidate/hypothesis parse that are present in the gold/reference parse
- Recall: the number of constituents in the gold/reference parse that are present in the candidate/hypothesis parse
- F-score: the harmonic mean of precision and recall

PARSEVAL (Black et al. 1991), a widely used evaluation script, also includes a measure that counts *crossing brackets*.

# Software

- Charniak (2000) is the best-known of the PCFG-plus-discriminative-reranking parsers and is still used for feature extraction (etc.)
- The BUBS "grammar-agnostic" parser (Bodenstab et al. 2011, Dunlop et al. 2011) is a good tradeoff between simplicity and generality, speed and accuracy; unfortunately it's in Java



# This week

Please read:

- Eisenstein ch. 10, and
- (optionally) Jurafsky & Martin ch. 12-14.

# Project ideas

- Implement either of the "Berkeley" parsers (Klein & Manning or Petrov et al.) and evaluate using the standard split of the Wall St. Journal portion of PTB-3.
- Perform a hybrid (automatic-manual) error analysis of prepositional phrase attachment ambiguity.
- Study the effects of morphological features in constituency parsing along the lines of Fraser et al. 2013, etc.